

# Helping Your Child with Integers, Rationals & Percentages

Number · Year 7 to Year 10 · Australian Curriculum Mathematics

In Years 7–10, your child extends their understanding of numbers well beyond whole numbers. They work with **integers** (positive and negative whole numbers), **rational numbers** (any number that can be written as a fraction), **percentages**, and eventually **irrational numbers** (like  $\sqrt{2}$  or  $\pi$ , which cannot be written as fractions). Percentages appear in every financial context — discounts, GST, interest, wages — making this topic very relevant to everyday life.

| Year   | What your child learns                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | What this looks like at home                                                                                                                                                                                                                                                                                                                                                                                                                           |
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| Year 7 | <p><b>Integers, rational numbers and percentages</b></p> <p><b>integer</b> — any whole number, positive, negative or zero: ...-3, -2, -1, 0, 1, 2, 3...</p> <p><b>rational number</b> — any number expressible as a fraction: <math>\frac{3}{4}</math>, 0.25, -2, 40%</p> <p>Your child adds and subtracts integers:<br/> <math>-3 + 7 = 4</math> , <math>5 - 8 = -3</math></p> <p>They convert between fractions, decimals and percentages:<br/> <math>\frac{3}{4} = 0.75 = 75\%</math></p> <p>They apply percentages to real problems:<br/> <math>20\% \text{ of } \\$85 = 0.20 \times \\$85 = \\$17</math></p> <p>They round decimals to required accuracy.</p>                                                                                                                 | <p><b>Temperature:</b> 'It was <math>-3^{\circ}\text{C}</math> overnight and rose <math>7^{\circ}</math>. What temperature is it now?'<br/> <math>(-3+7=+4^{\circ}\text{C})</math></p> <p><b>'A shirt costs \$60. There's a 25% discount. How much do you save?'</b><br/> <math>(0.25 \times 60 = \\$15 \text{ saving})</math></p> <p><b>'Convert <math>\frac{3}{5}</math> to a percentage.'</b><br/> <math>(\frac{3}{5} \times 100 = 60\%)</math></p> |
| Year 8 | <p><b>Irrational numbers and operations with all rational numbers</b></p> <p><b>irrational number</b> — cannot be written as a fraction:<br/> <math>\sqrt{2} = 1.41421...</math> (never ends, never repeats)<br/> <math>\pi = 3.14159...</math> (never ends, never repeats)</p> <p><b>terminating decimal</b> — ends after a set number of digits: <math>\frac{1}{4} = 0.25</math></p> <p><b>recurring decimal</b> — repeats forever: <math>\frac{1}{3} = 0.333...</math> (written <math>0.\dot{3}</math>)</p> <p>Your child uses all four operations with positive and negative fractions, decimals and percentages.</p> <p>Example: <math>-\frac{1}{2} + \frac{3}{4} = \frac{1}{4}</math> , <math>-2 \times -3 = 6</math> (negative <math>\times</math> negative = positive)</p> | <p><b>'Is <math>\sqrt{9}</math> rational or irrational?'</b><br/> <math>(\sqrt{9} = 3</math>, so rational — it's a whole number!)</p> <p><b>'Is <math>\sqrt{2}</math> rational or irrational?'</b><br/> (Irrational — 1.41421... goes on forever)</p> <p><b>'<math>1 \div 3 = 0.333...</math> — does it terminate or recur?'</b><br/> (it recurs)</p>                                                                                                  |
| Year 9 | <p><b>The real number system</b></p> <p><b>real number</b> — all numbers on the number line: rationals + irrationals combined</p> <p>The real number system:</p> <div data-bbox="240 1305 924 1702" data-label="Diagram"> </div> <p><b>Irrational numbers (<math>\sqrt{2}</math>, <math>\pi</math>) also belong to the real numbers</b></p> <p>Your child uses digital tools to work with all real numbers and solves problems involving irrational numbers:<br/> Area = <math>\pi \times r^2</math> uses <math>\pi</math> (irrational) but gives a real answer</p>                                                                                                                                                                                                                | <p><b>'Where does <math>-7</math> sit on the number line?'</b></p> <p><b>'Is 0.5 rational or irrational? What about 0.5050050005...?'</b></p> <p><b>'Use a calculator to find <math>\sqrt{7}</math>. Is the answer exact?'</b><br/> (Discuss: the calculator shows a rounded version — the true value keeps going.)</p>                                                                                                                                |

Year 10 on next page.

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| <b>Year 10</b> | <b>Approximation and its effects</b><br><b>exact value</b> — the precise answer, e.g. $\sqrt{2}$ or $\pi$<br><b>approximate value</b> — a rounded version, e.g. 1.414 or 3.14<br>Your child explores how rounding early in a chain of calculations can cause the final answer to be significantly wrong:<br><b>Exact:</b> $\sqrt{2} \times \sqrt{2} = 2$ (exactly)<br><b>Rounded:</b> $1.414 \times 1.414 = 1.999396$ (close, but not 2)<br><b>After 10 multiplications the error becomes significant.</b><br>In financial and scientific contexts, this matters a great deal.<br>To be 'exact' we often write answers in terms of $\pi$<br>$A = \pi \times 3^2 = 9\pi$ sq units | Use a calculator: multiply $1.414 \times 1.414$ .<br>'Is that exactly 2? What went wrong?'<br><br><b>'When should you keep the exact value (<math>\sqrt{2}</math>) and when is rounding OK?'</b><br><br>(Discuss: banking software uses exact values — rounding costs money!) |
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### ★ Fraction, decimal and percentage — three ways to write the same number

| Fraction      | Decimal | Percentage |  | Fraction      | Decimal | Percentage |
|---------------|---------|------------|--|---------------|---------|------------|
| $\frac{1}{2}$ | 0.5     | 50%        |  | $\frac{3}{4}$ | 0.75    | 75%        |
| $\frac{1}{4}$ | 0.25    | 25%        |  | $\frac{1}{5}$ | 0.2     | 20%        |

**Tip for percentages:** "Per cent" means per 100. So  $35\% = \frac{35}{100} = 0.35$ . To find a percentage of an amount: multiply by the decimal. e.g.  $35\% \text{ of } \$200 = 0.35 \times \$200 = \$70$ .

**Negative numbers rule:**  $\text{negative} \times \text{negative} = \text{positive}$  /  $\text{negative} \times \text{positive} = \text{negative}$  /  $\text{positive} + \text{negative} = \text{depends on size}$

# Helping at Home — Integers, Rationals & Percentages

Worked examples and questions to ask · Year 7 to Year 10

## How it works — worked examples

### Year 7 — Percentage discount

**A jacket costs \$120. It is 30% off. What is the sale price?**

|                       |                                                                               |
|-----------------------|-------------------------------------------------------------------------------|
| <b>Find 30%</b>       | 30% of \$120<br>$= 0.30 \times \$120 = \$36$ (the discount)                   |
| <b>Sale price</b>     | $\$120 - \$36 = \$84$                                                         |
| <b>OR in one step</b> | <b>70% of \$120</b><br>$= 0.70 \times \$120 = \$84$ (you pay 70% of original) |

### Year 7 — Adding and subtracting integers

**Townsville's temperature is 38°C. Darwin is 2°C cooler than Townsville. Alice Springs is 5°C colder than Darwin. What is the temperature is Alice Springs?**

|                      |                                                                               |
|----------------------|-------------------------------------------------------------------------------|
| <b>Darwin</b>        | $38 - 2 = 36^\circ\text{C}$<br>(2 degrees cooler than 38)                     |
| <b>Alice Springs</b> | $36 - 5 = 31^\circ\text{C}$<br>(5 degrees colder than Darwin)                 |
| <b>Number line</b>   | $38 \rightarrow 36 (-2) \rightarrow 31 (-5)$<br>Answer: Alice Springs is 31°C |

### Year 8 — Terminating and recurring decimals

**Convert these fractions to decimals and classify them:**

|               | Decimal                  | Type                                                   |
|---------------|--------------------------|--------------------------------------------------------|
| $\frac{1}{4}$ | 0.25                     | Terminating — stops after 2 decimal places             |
| $\frac{1}{3}$ | $0.333... = 0.\dot{3}$   | Recurring — the 3 repeats forever                      |
| $\frac{1}{6}$ | $0.1666... = 0.1\dot{6}$ | Recurring — the 6 repeats (1 is not part of the cycle) |

### Year 9 — Exact and approximate area (circles)

**A circular pond has a radius of 4 m. Find its exact area, then a decimal approximation.**

|                        |                                                                              |
|------------------------|------------------------------------------------------------------------------|
| <b>Exact area</b>      | Area $= \pi \times 4^2 = 16\pi \text{ m}^2$ (an exact answer — no rounding)  |
| <b>Decimal approx.</b> | $16\pi \approx 50.27 \text{ m}^2$ (rounded to 2 decimal places)              |
| <b>Why it matters</b>  | Both are correct — one is exact, the other is a practical, rounded estimate. |

## Questions to ask your child

*You don't need to solve these. Ask them and let your child explain their thinking!*

### 7 Year 7

- The temperature is  $-4^\circ\text{C}$  and drops 6 more degrees. What is the temperature now?
- A TV costs \$800. It's 15% off. How much is the discount? What's the sale price?
- Convert  $\frac{3}{5}$  to a decimal and then to a percentage.
- Order from smallest to largest:  $-3, 0.5, -0.7, 2, -1\frac{1}{2}$

### 8 Year 8

- Is 0.4 terminating or recurring? What fraction is it?
- Is  $\sqrt{5}$  rational or irrational? Why?
- What is  $-\frac{3}{4} + \frac{1}{2}$ ? (Convert to same denominator first.)
- Calculate  $-3 \times -4$ . What rule applies?

### 9 Year 9

- Where does  $\pi$  sit on the number line — between which two whole numbers?
- Is every integer a rational number? Why?
- Give an example of a real number that is NOT rational.
- Use a calculator to find  $\sqrt{10}$ . Is that answer exact?

*Year 10 on next page.*

## Year 10 — Exact vs rounded values

Compare using the exact value of  $\sqrt{2}$  with using a rounded (approximate) version in a calculation.

|                       |                                                                                                 |
|-----------------------|-------------------------------------------------------------------------------------------------|
| <b>Exact</b>          | $\sqrt{2} \times \sqrt{2} = 2$ (exactly — using the exact value throughout)                     |
| <b>Rounded</b>        | $1.414 \times 1.414 = 1.999396$ (close, but not exactly 2)                                      |
| <b>Why it matters</b> | In finance and science, rounding too early can cause errors to build up over many calculations. |

### 10 Year 10

- Multiply  $1.732 \times 1.732$ . Is the answer exactly 3? Why not?
- When is it better to keep the exact value (like  $\sqrt{3}$ ) rather than rounding?
- If you round  $\pi$  to 3.14 and use it 5 times in a calculation, how large might the error be?
- Find a real-life context where rounding too early causes a real problem.

## Things to try at home

|                                                                                                                                    |                                                                                                                                                                             |
|------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Year 7:</b> Check sale prices together when shopping. 'If this is 20% off, what's the original price? What do we actually pay?' | <b>Year 7:</b> Read a bank statement or electricity bill together. Point out negative numbers. 'What does -\$15 mean here?'                                                 |
| <b>Year 8:</b> Ask: 'Is $1 \div 7$ terminating or recurring?' Use the calculator to check. Count the decimal places together.      | <b>Year 8:</b> Discuss GST: 'If a price is \$44 including 10% GST, what was the price before GST?' ( $\div$ by 1.1)                                                         |
| <b>Year 9:</b> Look up current interest rates. 'If we borrow \$10,000 at 5.5% per year, how much interest is that per year?'       | <b>Year 9:</b> Use a calculator to find $\sqrt{2}$ , $\sqrt{3}$ and $\sqrt{5}$ . Notice the decimals never end or repeat — that's what makes them irrational!               |
| <b>Year 10:</b> Budget challenge: plan a family meal for \$50. Calculate percentages spent on each food type.                      | <b>Year 10:</b> Round $\pi$ to 3.14 and use it to estimate the circumference of a round table or plate ( $C = \pi d$ ). Then try 3.14159 — how much does the answer change? |

## Key words to learn together

|                                                                                                                                     |                                                                                                                                   |
|-------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------|
| <b>integer:</b> any whole number, positive, negative or zero: $\dots -3, -2, -1, 0, 1, 2, 3 \dots$                                  | <b>rational number:</b> any number that can be written as a fraction (ratio of two integers): $\frac{3}{4}, -2, 0.5, 40\%$        |
| <b>irrational number:</b> a number that CANNOT be written as a fraction: $\sqrt{2}, \sqrt{3}, \pi$ (go on forever, never repeating) | <b>real number:</b> all numbers on the number line: rationals AND irrationals combined                                            |
| <b>percentage:</b> a number out of 100: $35\% = \frac{35}{100} = 0.35$                                                              | <b>terminating decimal:</b> a decimal that ends: $\frac{1}{4} = 0.25$ (terminates after 2 places)                                 |
| <b>recurring decimal:</b> a decimal that repeats forever:<br>$\frac{1}{3} = 0.333\dots$ — shown as $0.\dot{3}$                      | <b>discount:</b> a reduction in price, often expressed as a percentage                                                            |
| <b>GST:</b> Goods and Services Tax — an extra 10% added to prices in Australia                                                      | <b>approximate value:</b> a rounded version of a number, e.g. $\pi \approx 3.14$                                                  |
| <b>exact value:</b> the precise value with no rounding, e.g. $\pi$ or $\sqrt{2}$                                                    | <b>square root:</b> a number that when multiplied by itself gives the original number: $\sqrt{9} = 3$ (because $3 \times 3 = 9$ ) |